

$$a^m \times a^n = a^{m+n} \quad (a^m b^n)^p = a^{mp} b^{np}$$

$$\frac{a^m}{a^n} = a^{m-n} \quad \left(\frac{a^m}{b^n}\right)^p = \frac{a^{mp}}{b^{np}}$$

$$(a^m)^n = a^{mn} \quad a^0 = 1$$

Numbers, Radicals, and Exponents

LESSON FIVE - *Exponents I*

Lesson Notes

Introduction Exponent Laws I

a) Product of Powers

$$2^3 \times 2^4 = \left(\frac{3}{4}\right)^5 \left(\frac{3}{4}\right)^2 =$$

General Rule:

b) Quotient of Powers

$$(-6)^8 \div (-6)^5 = \frac{7^9}{7^7} =$$

General Rule:

c) Power of a Power

$$(2^5)^3 = ((-3)^2)^4 =$$

General Rule:

d) Power of a Product

$$(a^2 b^5)^3 = (4a^3 b^2)^4 =$$

General Rule:

e) Power of a Quotient

$$\left(\frac{a^3}{b^5}\right)^3 = \left(\frac{2a^6}{3b^4}\right)^3 =$$

General Rule:

f) Exponent of Zero

$$2^0 = \left(\frac{3mn^2}{7p^6q^4}\right)^0 =$$

General Rule:

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$$\begin{array}{ll} a^m \times a^n = a^{m+n} & (a^m b^n)^p = a^{mp} b^{np} \\ \frac{a^m}{a^n} = a^{m-n} & \left(\frac{a^m}{b^n}\right)^p = \frac{a^{mp}}{b^{np}} \\ (a^m)^n = a^{mn} & a^0 = 1 \end{array}$$

Example 1

Simplify each of the following expressions.

a) $2^3 \times 2^4$

b) $\frac{3^9}{3^6}$

c) $\left(\frac{2a^2}{b}\right)^3$

d) $3(3^5)$

e) $\frac{7^4}{7}$

f) $(3a^2)^3$

$$\begin{array}{ll} a^m \times a^n = a^{m+n} & (a^m b^n)^p = a^{mp} b^{np} \\ \frac{a^m}{a^n} = a^{m-n} & \left(\frac{a^m}{b^n}\right)^p = \frac{a^{mp}}{b^{np}} \\ (a^m)^n = a^{mn} & a^0 = 1 \end{array}$$

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Example 2

Simplify each of the following expressions.

a) $5(3a^2b)$

b) $(4a)(4b^2)$

c) $(7a^2b^5)(-3ab^6)$

d) $\frac{36ab^2}{6b}$

e) $\frac{10a^8b}{15a^6c}$

f) $\frac{(3ab)(2ab)^2}{2(ab)^3}$

Numbers, Radicals, and Exponents

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$$\begin{array}{ll} a^m \times a^n = a^{m+n} & (a^m b^n)^p = a^{mp} b^{np} \\ \frac{a^m}{a^n} = a^{m-n} & \left(\frac{a^m}{b^n}\right)^p = \frac{a^{mp}}{b^{np}} \\ (a^m)^n = a^{mn} & a^0 = 1 \end{array}$$

Example 3

Simplify each of the following expressions.

a) $(3a^2b^3)^2$

b) $\left(\frac{4a}{5b}\right)^2$

c) $\left(\frac{16a^2b^5}{20ab^3}\right)^3$

d) $\left(-\frac{3a}{2b}\right)^0$

e) $\left(\frac{2a}{b}\right)^2 (ab)^0 \left(-\frac{1}{2}\right)^3$

f) $\frac{1}{25a^6} (5a^5)^2$

$$\begin{array}{ll} a^m \times a^n = a^{m+n} & (a^m b^n)^p = a^{mp} b^{np} \\ \frac{a^m}{a^n} = a^{m-n} & \left(\frac{a^m}{b^n}\right)^p = \frac{a^{mp}}{b^{np}} \\ (a^m)^n = a^{mn} & a^0 = 1 \end{array}$$

Numbers, Radicals, and Exponents

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Example 4

For each of the following, find a value for m that satisfies the equation.

a) $(a^2)^m = a^{10}$

b) $a^{2m} \times a^8 = a^{14}$

c) $\left(\frac{a^7}{a^{3m}}\right) = a$

d) $\left(\frac{a^m \times a^{2m}}{a}\right) = a^{20}$