

## Relations and Functions LESSON ONE - Graphing Relations Lesson Notes

## Introduction Caitlin rides her bike to school every day. The table of values below shows her distance from home as time passes.

a) Write a sentence that describes this relation.
b) Represent this relation with ordered pairs.
c) Represent this relation with an arrow diagram.


| time <br> (minutes) | distance <br> (metres) |
| :---: | :---: |
| 0 | 0 |
| 1 | 250 |
| 2 | 500 |
| 3 | 750 |
| 4 | 1000 |
| 5 | 1250 |

d) Write an equation for this scenario.
e) Graph the relation.


Example 1
For each relation, complete the table of values and draw the graph.
a) $y=-2 x+3$

| $x$ | $y$ |
| :---: | :---: |
| -2 |  |
| -1 |  |
| 0 |  |
| 1 |  |
| 2 |  |


b) $y=x$

| $x$ | $y$ |
| :---: | :---: |
| -2 |  |
| -1 |  |
| 0 |  |
| 1 |  |
| 2 |  |



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| Graph |
| :---: |
| $y=x^{2}$ |


| $x$ | $y$ |
| :---: | :---: |
| -2 | 4 |
| -1 | 1 |
| 0 | 0 |
| 1 | 1 |
| 2 | 4 |

## Example 2

For each relation, complete the table of values and draw the graph. State if the relation is linear or non-linear.
a) $y=x^{2}$
b) $y=\frac{1}{2} x+1$

| $x$ | $y$ |
| :---: | :---: |
| -2 |  |
| -1 |  |
| 0 |  |
| 1 |  |
| 2 |  |




For each scenario, state the dependent variable, the independent variable, and the rate. Write the equation.
a) A fruit vendor generates a revenue of $R$ dollars by selling $n$ boxes of plums at $\$ 3$ each.
i) the dependent variable is $\qquad$ .
ii) the independent variable is $\qquad$ .
iii) the rate is $\qquad$ .
iv) the equation is $\qquad$ .
b) A runner with a speed of $9 \mathrm{~m} / \mathrm{s}$ can run $d$ metres in $t$ seconds.
i) the dependent variable is $\qquad$ .
ii) the independent variable is $\qquad$ .
iii) the rate is $\qquad$ .
iv) the equation is $\qquad$ .
c) A diver experiences a pressure of $P$ kilopascals at a depth of $d$ metres. Underwater pressure increases at 10 kilopascals/metre.
i) the dependent variable is $\qquad$ .
ii) the independent variable is $\qquad$ .
iii) the rate is $\qquad$ .
iv) the equation is $\qquad$ -

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## Example 4

 Tickets to a concert cost $\$ 12$ each. The revenue from ticket sales is $R$, and the number of tickets sold is $n$.a) Write an equation for this scenario.
b) Generate a table of values.
c) Draw the graph.


| $n$ | $R$ |
| :---: | :---: |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |


d) Is the relation continuous or discrete?

## Example 5

A cylindrical tank is being filled with water at a rate of $3 \mathrm{~L} / \mathrm{min}$. The volume of water in the tank is $V$, and the elapsed time is $t$.
a) Write an equation for this scenario.
b) Generate a table of values.
c) Draw the graph.


Example 6 A relation is represented by $4 x+2 y=8$.
a) Isolate $y$ so this relation can be graphed.
b) Generate a table of values.

| $x$ | $y$ |
| :---: | :---: |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |

d) Is the relation
continuous or discrete?

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## Graph <br> $y=x^{2}$

| $x$ | $y$ |
| :---: | :---: |
| -2 | 4 |
| -1 | 1 |
| 0 | 0 |
| 1 | 1 |
| 2 | 4 |

## Example 7

Nick, a salesman, earns a base salary of $\$ 600 /$ week
plus an $8 \%$ commission on sales. The amount of money Nick earns in a week is $E$, and the total value of his sales is $s$.
a) Write an equation that relates the variables.
b) Complete the table of values.

| $\boldsymbol{s}$ | $\boldsymbol{E}$ |
| :---: | :---: |
| 0 |  |
| 1000 |  |
| 2000 |  |
| 3000 |  |
| 4000 |  |

c) Draw the graph.

h) How much will Nick have to sell if he makes \$1560 in one week?
d) Is this relation linear or non-linear?
e) Is this relation discrete or continuous?
f) What are the dependent and independent variables?

