**Chapter 3: Set Theory and Logic** <u>Vocabulary and Symbols</u>

Key

# 3.1 Types of Sets and Set Notation

Term	Definition	Example
Set	A collection of distinguishable <u>objects</u> . Sets are defined using brackets.	The set of whole numbers is: $W = \{0, 1, 2, 3, \dots, 3\}$
Element	An <u>object</u> in a set	
Universal Set	A set of <u>all</u> the elements under consideration for a particular context. (Also called <u>sample space</u> )	The universal set (or sample space) of digits is: $D=\{0,1,2,3,4,5,6,7,8,9\}$
Subset	A set whose elements <u>all belong</u> to <u>another</u> <u>set</u> . To show A is a subset of B, we write $A \subset B$ $\uparrow$ $\uparrow$ is a subset of "	The set of odd digits, $O = \underbrace{\xi 1, 3, 5, 7, 9 \underbrace{\xi}_{D}$ is a subset of <i>D</i> , the set of digits. In set notation, this is written $O \subseteq D$
Complement	All the elements of a universal set that $do \underline{od}$ belong to a subset of it. The complement is denoted with a prime sign $A'$ or a horizontal bar above, $\overline{A}$ .	$O' = \underbrace{20, 2, 4, 6, 8}_{\text{Is the complement of}}$ Is the complement of $O = \{1, 3, 5, 7\}$ , a subset of the universal set of digit, <i>D</i> .
Empty Set	A set with <u>of</u> <u>elements</u> The empty set is denoted by { } or Ø.	Q, the set of odd numbers divisible by 2 is the <u>empty</u> set. In set notation, this is written: $Q = \frac{2}{3}$ or $Q = \frac{2}{3}$

Term	Definition	Example
Disjoint	Two or more sets having elements in	The set of even numbers and the set of numbers are disjoint.
Finite set	A set with a <u>Countable</u> number of elements	The set of even numbers less than 10 E=32.4,6.83
Infinite set	A set with an <u>infinite</u>	The set of natural numbers, N=Z1,2,3,Z
n(X)	The <u>number</u> of elements of the set <i>X</i> .	If the set X is defined as the set of numbers from 1 to 5, $X = \{1,2,3,4,5\}$ n(X) = 5
Mutually Exclusive	Two or more events that <u>connot</u> at the same time.	The sun rising + the sun setting are mutually exclusive

# 3.3 Intersection and Union of Two Sets

Term	Definition	Example
Intersection	The set of elements that are <u>COMMON</u> to two or more sets. In set notation, the intersection of sets <i>A</i> and <i>B</i> is: <u>A A</u>	If $A = \{1, 2, 3\}$ and $B = \{3, 4, 5\}$ , then $A \cap B = \underbrace{333}_{333}$
Union	The set of <u>all</u> the elements in two or more sets. In set notation, the union of sets and <i>B</i> is: <u>AUB</u>	If $A = \{1, 2, 3\}$ and $B = \{3, 4, 5\}$ , then $A \cup B = \underbrace{\frac{1}{2}, \frac{2}{3}, \frac{4}{5}}_{3}$
Αιβ	Elements in set A but not in set B	$A \ B = \frac{2}{3} \frac{3}{5} \frac{4}{8}$

## Foundations of Math 12

## **3.5** Conditional Statements and Their Converse

Term	Definition	Example
Conditional	An <u>"if - then</u> statement	If it is Monday
Statement		Then it is a school day
Hypothesis	An assumption	From above
JI		"It is Monday" is
		the hypothesis
Conclusion	The <u>result</u> of a hypothesis	From above "It is a school day"
		is the conclusion
Counterexample	An example that discocoules a	From above
e o univer en ampre	statement.	manksgiving nonady
	A conditional statement in which the	From above
Converse	hypothesis and the	"If it is a school day
	<u>conclusion</u> are switched.	then it is Monday"
Biconditional	A conditional statement whose converse is	The statement: "If a number is
	also <u>true</u> . In logic	even then it is divisible by 2" is
	notation, a biconditional statement is	true. The converse "If a number
	written as " $p$ if and only if $q$ "	is divisible by 2, then it is even"
		is also true. The biconditional
		statement is: <u>"A number</u>
		is even if and only if
		IT IS divisible by 2
$p \Rightarrow q$	Notation for <u>"If p, then q"</u>	
	Is read as "p implies q"	
$p \Leftrightarrow q$	Notation for <u>pif and only if q</u> "	
	means both the conditional r statement and its converse	

#### Foundations of Math 12

Term	Definition	Example
Inverse	A statement that is formed by both the hypothesis and the conclusion of a conditional statement.	"If a number is even, then it is divisible by 2." The inverse is: <u>"If a number</u> <u>is not even, then it is</u> <u>not divisible by 2"</u>
Contrapositive	A statement that is formed by <u>negating</u> both the hypothesis and the conclusion of the <u>converse</u> of a conditional statement.	"If a number is even, then it is divisible by 2." The contrapositive is: <u>"If a</u> <u>number is not divisible</u> by 2, then it is not even"
$\neg p$	"not" p	

5.0 The inverse and the Contrapositive of Conditional Statements	3.6	The Inverse a	nd the Contra	positive of Co	nditional Statem	ients
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	Name
	Date
	Goal: Understand sets and set notation.
1.	set: A collection of distinguishable objects; for example, the set of whole numbers is W = {0, 1, 2, 3,}.
2.	element: An object in a set; for example, 3 is an element of D, the set of digits.
3.	<b>universal set:</b> A set of all the elements under consideration for a particular context (also called the sample space); for example, the universal set of digits is $D = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9\}$ .
4.	<b>subset:</b> A set whose elements all belong to another set; for example, the set of odd digits, $O = \{1, 3, 5, 7, 9\}$ , is a subset of $D$ , the set of digits. In set notation, this relationship is written as: $O \subset D$ .
5.	<b>complement:</b> All the elements of a universal set that do not belong to a subset of it; for example, $O' = \{0, 2, 4, 6, 8\}$ is the complement of $O = \{1, 3, 5, 7, 9\}$ , a subset of the universal set of digits, <i>D</i> . The complement is denoted with a prime sign, <i>O'</i> .
6.	empty set: A set with no elements; for example, the set of odd numbers divisible by 2 is the empty set. The empty set is denoted by { } or Ø.
7.	disjoint: Two or more sets having no elements in common; for example, the set of even numbers and the set of odd numbers are disjoint.
8.	<b>finite set</b> : A set with a countable number of elements; for example, the set of even numbers less than 10, $E = \{2, 4, 6, 8\}$ , is finite.
9.	<b>infinite set:</b> A set with an infinite number of elements; for example, the set of natural numbers, $N = \{1, 2, 3,\}$ , is infinite.
10.	mutually exclusive: Two or more events that cannot occur at the same time; for example, the Sun rising and the Sun setting are mutually exclusive events.

#### INVESTIGATE the Math

Jasmine is studying the provinces and territories of Canada. She has decided to categorize the provinces and territories using **sets**.



How can Jasmine use sets to categorize Canada's regions?

A. List the elements of the universal set of Canadian provinces and territories, C.

C - { YT, NT, NU, BC, AB, SK, MB, ON, QC, NB, NS, PE, NL }

B. One subset of C is the set of Western provinces and territories, W. Write W in set notation.

N= {YT, NT, NU, BC, AB, SK, MB3



- C. The Venn diagram above represents the universal set, C. The circle in the Venn diagram represents the subset W. The **complement** of W is the set W'.
  - i. Describe what W'contains.

W' contains all these provinces and territories that aren't W

ii. Write W'in set notation.

iii. Explain what W'represents in the Venn diagram.

D. Jasmine wrote the set of Eastern provinces as follows: E = {NL, PE, NS, NB, QC, ON} is E equal to V? Explain.

"" Jes, some elements are in both subsets W1'2

E. List *T*, the set of territories in Canada. Is *T* a subset of C? Is it a subset of *W*, or a subset of *W*? Explain using your Venn diagram.

T is a subset W T= { YT, NT, NU} and C TCW TCC

F. Explain why you can represent the set of Canadian provinces south of Mexico by the empty set . There are no provinces south of MX G. Consider sets C, W, W', and T. List a pair of disjoint sets. Is there more than one pair of disjoint sets? W' and T are disjoint W and W' are disjoint H. Complete your Venn diagram by listing the elements of each subset in the appropriate circle. P.147 Communication Notation The following is a summary of notation introduced so far. Sets are defined using brackets. For example, to define the universal set of the numbers 1, 2, and 3, list its elements: p.150  $U = \{1, 2, 3\}$ To define the set A that has the numbers 1 and 2 as elements: A = {1, 2} nunication Notation  $1 \le x \le 5$ All elements of A are also elements of U, so A is a subset of U. The phrase "from 1 to 5" means "from 1 to 5 inclusive." ACU in set notation, the number of elements of the set X is The set A', the complement of A, can be defined as: written as n(X).  $A' = \{3\}$ For example, if the set X is defined as the set of numbers from 1 to 5: To define the set B, a subset of U that contains the number 4:  $B = \{ \}$  or  $B = \emptyset$  $B \subset U$  $X = \{1, 2, 3, 4, 5\}$ n(x) = 5

Example 1: Sorting numbers using set notation and a Venn diagram (p.148)

- a) Indicate the multiples of 5 and 10, from 1 to 500, using set notation. List any subsets.
- b) Represent the sets and subsets in a Venn diagram.

a) Short with a universal set, is what types of  
numbers are multiples of 5 and 10?  

$$S = \{1,2,3,...,494,499,500\}$$

$$S = \{2,1,1232500, x \in N\}$$

$$T = \{5,10,15,20,...,470,495,500\}$$

$$F = \{5,15,52,132500, x \in N\}$$

$$T = \{10,20,30,...,470,495,500\}$$

$$T = \{10,20,30,...,470,495,500\}$$

$$T = \{t,t-10x,15x550,200N\}$$

$$T = \{t,t-10x,15x550,200N\}$$

$$T = F < 5$$

$$F^{1} = 1000-1000 \text{ types of 5}$$
b)









#### HW: 3.1 p. 154-158 #4, 6, 8, 9, 11, 12, 14, 15, 16 & 19

	Name
	Date
Goa	I: Explore what the different regions of a Venn diagram represent.
EXPLORE t	he Math
In an Alberta 26 play bask diagram rep	i school, there are 65 Grade 12 students. Of these students, 23 play volleyball and setball. There are 31 students who do not play either sport. The following Venn resents the sets of students.
	S (all Grade 12 students) = 65
V	(volleyball) $(5-3)=34$
	23-15=8 26-15=11
	V  or  B = 34
	72 + 26 = 49
2	B (basketball)
	49-34=15
How many s	tudents play: Volleyball only? Both Volleyball and Basketball?
	Basketball only? Neither sport?
Reflect: Con bas	sider the set of students who play volleyball and the set of students who play ketball. Are these two sets disjoint? Explain how you know.
	No lossing the a is overlap in the sets of
	because there is one of the
	the Venn diagram



Example 3: In a high school, there are 130 grade 11 students. Currently, 82 students are taking math, 27 are taking math and physics, 25 are taking math and chemistry, 20 are taking chemistry and physics, 110 are taking math or chemistry, and 87 are taking chemistry or physics. Eleven students are taking all three courses.

a) Draw a Venn diagram to display the information.



$$\begin{array}{l} 27 - 11 = 16\\ 25 - 11 = 14\\ 20 - 11 = 9\\ 82 - 16 - 16 - 16 - 14 = 41\\ 110 - 41 - 16 - 11 - 14 - 9 = 19\\ 87 - 19 - 14 - 11 - 9 - 16 = 18\end{array}$$

b) How many students are taking math or physics?

c) How many students are taking none of these three courses?

130-41-16-11-14-19-9-14=2

Example 4: Each student at a music camp plays at least one of the following instruments: violin, piano, or saxophone. It is known that 6 students play all three instruments, 163 play piano, 36 play piano and violin, 13 play piano and saxophone, 11 play saxophone and violin, 208 play violin or piano, and 98 play saxophone or violin.

a) Draw a Venn diagram to display the information.

$$V$$
  $40$   $30$   $120$   
 $5$   $7$   
 $10$   $5$ 

b) How many students are there at the camp?



Dete Goal: Understand and represent the intersection and union of two sets. Intersection: The set of elements that are common to two or more sets. In set notation, $A \cap B$ denotes the intersection of sets $A$ and $B$ ; for example, if $A = \{1, 2, 3\}$ and $B = \{3, 4, 5\}$ , then $A \cap B = \{3\}$ . Intersection: The set of all the elements in two or more sets; in set notation, $A \cup B$ denotes the union of sets $A$ and $B$ ; for example, if $A = \{1, 2, 3\}$ and $B = \{3, 4, 5\}$ , then $A \cup B = \{1, 2, 3, 4, 5\}$ . Principle of Inclusion and Exclusion: The number of elements in the union of two sets is equal to the sum of the number of elements in each set, less the number of elements in both sets; using set notation, this is written as $n(A \cup B) = n(A) + n(B) - n(A \cap B)$ . Principle of Inclusion and Exclusion: The number of all sets the number of elements in both sets; using set notation, this is written as $n(A \cup B) = n(A) + n(B) - n(A \cap B)$ . Principle of Inclusion and Exclusion: The number of all sets the number of elements in the union of two sets is equal to the sum of the number of elements in each set, less the number of elements in both sets; using set notation, this is written as $n(A \cup B) = n(A) + n(B) - n(A \cap B)$ . Principle of Inclusion and Exclusion: The number of all as "union of A and B." It denotes the elements that a common to the denotes the elements that are inset. Principle of the two degree network of $A = n(B + n(B) - n(B) - n(A \cap B)$ . Principle of the two degree network of $A = n(B + n(B) - n(B) - n(B) - n(B - n(B))$ . Principle of the two degree network of $A = n(B + n(B) - n$	<text><list-item><list-item><list-item></list-item></list-item></list-item></text>	<text><list-item><list-item><list-item><list-item></list-item></list-item></list-item></list-item></text>		Name
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It denotes the elements that are common to a set as the origin in the Ven digram blow.</li> <li>A D B is read as "union of A and B." It denotes the elements that are common to a set as the elements that are common to a set as the elements that are common to a set as the elements that are common to a set as the denotes that being to at least one of A.</li> <li>B The transaction of A = B the intersection of A = B the red as "union of A and B." It denotes the two digram blow.</li> <li>A U B is read as "A minus B." It denotes the set of elements that are in set A but not in set B. It is the red region in the Ven digram blow.</li> <li>A B is read as "A minus B." It denotes the set of elements that are in set A but not in set B. It is the red region in each Ven digram blow.</li> <li>A b is med as "A minus B." It denotes the set of elements that are in set A but not in set B. It is the red region in each Ven digram blow.</li> <li>A b is med as B = A minus B." 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Principle of Inclusion and Exclusion: The number of elements in the union of two sets is equal to the sum of the number of elements in each set, less the number of elements in both sets; using set notation, this is written as <i>n</i>(<i>A</i> ∪ <i>B</i>) = <i>n</i>(<i>A</i>) + <i>n</i>(<i>B</i>) - <i>n</i>(<i>A</i> ∩ <i>B</i>).</li> <li>3. Frinciple of Inclusion and Exclusion: The number of alements in the union of two sets is equal to the sum of the number of elements in each set, less the number of elements in both sets; using set notation, this is written as <i>n</i>(<i>A</i> ∪ <i>B</i>) = <i>n</i>(<i>A</i>) + <i>n</i>(<i>B</i>) - <i>n</i>(<i>A</i> ∩ <i>B</i>).</li> <li>3. For notion, A P B read as "framework" a <i>P</i> is <i>P</i> is <i>n</i>(<i>A</i> ∪ <i>B</i> is need as "unon of <i>A</i> and <i>B</i>." It denotes the elements that are common to all advections are associated in the Ven diagram below.</li> <li>3. A elements that abelong to at least or of <i>A</i> and <i>B</i>." It denotes the elements that the bind to at least one of <i>A</i> and <i>B</i>." The mutation the read elements that the length of a least as <i>C</i>.</li> <li>4. J is not at <i>C</i>.</li> <li>5. J is not at <i>C</i>.</li> <li>5. J is not at <i>C</i>.</li> <li>5. J is not at <i>C</i>.</li> <li></li></ul>	<ul> <li>1. intersection: The set of elements that are common to two or more sets. In set notation, A ∩ B denotes the intersection of sets A and B; for example, if A = {1, 2, 3} and B = {3, 4, 5}, then A ∩ B = {3}.</li> <li>2. union: The set of all the elements in two or more sets; in set notation, A ∪ B denotes the union of sets A and B; for example, if A = {1, 2, 3} and B = {3, 4, 5}, then A ∪ B = {1, 2, 3, 4, 5}.</li> <li>3. 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<ul> <li>2. union: The set of all the elements in two or more sets; in set notation, A ∪ B denotes the union of sets A and B; for example, if A = {1, 2, 3} and B = {3, 4, 5}, then A ∪ B = {1, 2, 3, 4, 5}.</li> <li>3. Principle of Inclusion and Exclusion: The number of elements in the union of two sets is equal to the sum of the number of elements in each set, less the number of elements in both sets; using set notation, this is written as n(A ∪ B) = n(A) + n(B) - n(A ∩ B).</li> <li>Vertication I Votation A B is read as "intersection of to A and B." It denotes the elements that are common to A and B. The intersection is the region where the verticagement box. A UB is read as "intersection is the region where the verticagement box. A UB is read as "intersection is the region where the verticagement box. A UB is read as "A minus B." It denotes the set of elements that are in set A but not in set B. It the reference that are in set A but not in set B. 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Principle of Inclusion and Exclusion</b>: The number of elements in the union of two sets is equal to the sum of the number of elements in each set, less the number of elements in both sets; using set notation, this is written as n(A ∪ B) = n(A) + n(B) - n(A ∩ B).</li> <li><b>Communication</b> Notation</li> <li>A of B is read a "Intersction of A and B." It denotes the demonst but between the two sets overlap in the Vien diagram below.</li> <li>A of B. The interaction is the regression where the two sets overlap in the Vien diagram below.</li> <li>A of B. The start as the of region in the Vien diagram below.</li> <li>A of B. The start as the are ommony.</li> <li>A of B. The start as the are in set A but not in set B. The two is the agam below.</li> <li>A when B = A minus B. The denotes the at end region in the Vien diagram below.</li> <li>A of B. The minus B at the are in set A but not in set B. The two is the diagram below.</li> <li>A when B = A minus B. The denotes the at a in set A but not in set B. The two is the diagram below.</li> <li>A when B = A minus B. The denotes the at a lister of the model means the set of elements the at end region in the Vien diagram below.</li> <li>A when B = A minus B. The denotes the at of elements the at end to the set B. The vien of the diagram below.</li> <li>A when B = A minus B. The denotes the et at of elements the two is set A but not in set B. The two is the diagram below.</li> <li>A when B = A minus B. The denotes the diagram below.</li> <li>A when B = A minus B. The denotes the diagram below.</li> <li>A when B = A minus B. The denotes the diagram below.</li> <li>A when B = A minus B. The denotes the diagram below.</li> <li>A when B = A minus B. The denotes the diagram below.</li> <li>A when B = A minus B. The denotes the dis the dis the diagram below.</li> <li></li></ul>	<ul> <li>a. union: The set of all the elements in two or more sets; in set notation, A ∪ B denotes the union of sets A and B; for example, if A = {1, 2, 3} and B = {3, 4, 5}, then A ∪ B = {1, 2, 3, 4, 5}.</li> <li><b>7. Principle of Inclusion and Exclusion</b>: The number of elements in the union of two sets is equal to the sum of the number of elements in each set, less the number of elements in both sets; using set notation, this is written as n(A ∪ B) = n(A) + n(B) - n(A ∩ B).</li> <li><b>7. Formulation</b> Notation</li> <li><b>1. But notation</b>, A ∩ B is read as "infrarection of A of B. and B. " If denotes the elements that belong to the set of elements in the vent days the set of a denotes to set overlap in the Vent days the elements that belong to the set of a denotes the set of elements that belong to the set of a denote set of a denote set of the read as " the onder set of the onder set of the onder set of the read as " the onder set of the elements that belong to the set of the denotes the set of elements that belong to the set of elements that belong the vent days the box.</li> <li><b>1. But notation 1. But notat</b></li></ul>	1.	<b>intersection</b> : The set of elements that are common to two or more sets. In set notation, $A \cap B$ denotes the intersection of sets A and B; for example, if $A = \{1, 2, 3\}$ and $B = \{3, 4, 5\}$ , then $A \cap B = \{3\}$ .
<ul> <li>A. Principle of Inclusion and Exclusion: The number of elements in the union of two sets is equal to the sum of the number of elements in each set, less the number of elements in both sets; using set notation, this is written as n(A ∪ B) = n(A) + n(B) - n(A ∩ B).</li> <li>A. S. Tornunication Notation</li> <li>A. S. B is read as "intersection of Ar and B." the denotes in the view of elements that are common is the region where the two sets covering in the Venn diagram below.</li> <li>A. B. B is read as "intersection of B is the region in the Venn is the region in the Venn diagram below.</li> <li>A. B. B is read as "A minus B." It denotes the set of elements that are in set A but not in set B. Its the region in each Venn diagram below.</li> <li>A. B is read as "A minus B." It denotes the set of elements that are in set A but not in set B. Its the region in each Venn diagram below.</li> <li>A. B is mean as "A minus B." It denotes the set of elements that are in set A but not in set B. Its the region in each Venn diagram below.</li> <li>A. B when B ⊂ A</li> <li>A. B when a true and pilon A</li> <li>A. B when they are diajon A</li> <li>A. B when they are diajon A</li> <li>A. B when they are diajon A</li> <li>A. B when they are the diagram below.</li> </ul>	<b>1.</b> Principle of Inclusion and Exclusion: The number of elements in each set, less the number of elements in to the sets; using set notation, this is written as n(A ∪ B) = n(A) + n(B) - n(A ∩ B). <b>1.</b> Principle of Inclusion and Exclusion: The number of elements in each set, less the number of elements in to the sets; using set notation, this is written as n(A ∪ B) = n(A) + n(B) - n(A ∩ B). <b>1.</b> Principle of Inclusion and Exclusion: The number of elements that beiong to A and B. The inclusion of A and B. The inclusion is the regroups are box. <b>1.</b> Principle of the the elements that are common to A and B. The inclusion is the regroups are box. <b>1.</b> Principle of the the elements that are common to a set at B. The inclusion is the reference in the Vendagame below. <b>1.</b> Principle of the the elements that are common of A and B. The there are region in the Vendagame below. <b>1.</b> Principle of the there are an a the regroup in the Vendagame below. <b>1.</b> Principle of the there are an are on the there are an an area. <b>1.</b> Principle of the there area area. <b>1.</b> Principle of the there area. <b>1.</b> Principle	<ul> <li><b>1.</b> Principle of Inclusion and Exclusion: The number of elements in the union of two sets is upon the number of elements in each set, less the number of elements in the sets is upon the number of elements in each set, less the number of elements in the sets is upon the number of elements in each set, less the number of elements in the sets is upon the number of elements in each set, less the number of elements in the sets is upon the number of elements in each set. If the number of elements in the sets one of a data of the number of elements that being to at least one of a data of the number of elements the number</li></ul>	2.	<b>union</b> : The set of all the elements in two or more sets; in set notation, $A \cup B$ denotes the union of sets A and B; for example, if $A = \{1, 2, 3\}$ and $B = \{3, 4, 5\}$ , then $A \cup B = \{1, 2, 3, 4, 5\}$ .
				in both sets; using set notation, this is written as $n(A \cup B) = n(A) + n(B) - n(A \cap B)$ . <b>Communication Notation</b> The st notation, $A \cap B$ is read as "intersection of A and B." It denotes the elements that are common to and B. The intersection is the region where the vo sets overlap in the Venn diagram below. <b>A</b> $O B$ is read as "union of A and B." It denotes al elements that belong to at least one of A or B. The union is the red region in the Venn diagram below. <b>A</b> $O B$ is read as "union of A and B." It denotes al elements that belong to at least one of A or B. The union is the red region in the Venn diagram below. <b>A</b> $O B$ is read as "A minus B." It denotes the set of elements that are in set A but not in set B. It is the red region in each Venn diagram below. <b>A</b> $O B$ is read as "A minus B." It denotes the set of elements that are in set A but not in set B. It is the red region in each Venn diagram below. <b>A</b> $O B$ is mean as "A minus B." It denotes the set of elements that are in set A but not in set B. It is the red region in each Venn diagram below. <b>A</b> $O B$ is mean as "A minus B." It denotes the set of elements that are in set A but not in set B. <b>A</b> $O B$ is mean as "A minus B." It denotes the set of elements that are in set A but not in set B. <b>A</b> $O B$ is mean as "A minus B." It denotes the set of elements that are in set A but not in set B. <b>A</b> $O B$ is mean as "A minus B." It denotes the set of elements that are in set A but not in set B. <b>A</b> $O B$ is mean as "A minus B." It denotes the set of elements that are in set A but not in set B. <b>A</b> $O B$ is mean as "A minus B." It denotes the set of elements that are in set A but not in set B. <b>A</b> $O B$ is mean as "A minus B." It denotes the set of elements that below. <b>A</b> $O B$ is mean as "A minus B." It denotes the set of elements that below. <b>A</b> $O B$ is mean as "A minus B." It denotes the set of elements that below. <b>A</b> $O B$ is mean as "A minus B." It denotes the set of elements that below. <b>A</b> $O B$ is mean as











		Name
		Date
Goal:	Use sets to model and solve pro	blems.
Example 1: Se	olving a puzzle using the Principle	e of Exclusion and Inclusion (p.180)
Use the follow	ving clues to answer the questions	s below:
<ul> <li>28 child bird.</li> <li>13 child</li> <li>13 child</li> <li>13 child</li> </ul>	dren have a dog, a cat, or a <b>n ( βしこしっ)</b> dren have a dog. dren have a cat. dren have a bird.	<ul> <li>4 children have only a dog and a cat.</li> <li>3 children have only a dog and a bird.</li> <li>2 children have only a cat and a bird.</li> <li>No child has two of each type of pet.</li> </ul>
a) How many	children have a cat, a dog, and a	a bird?
Define the set Let <i>x</i> represe with a bird, a $P = \{ child \\ C = \{ child \\ B = \{ child \\ D = \{ child \} \}$	ats and draw a Venn diagram. and the number of children a cat, and a dog. dren with $pers$ dren with a <u>cat</u> dren with a <u>bird</u> dren with a <u>log</u>	$ \begin{array}{c}     13 = B \\     7 \\     3 \\     4   \end{array} $ $ \begin{array}{c}     P \\     7 \\     5   \end{array} $ $ \begin{array}{c}     P \\     7 \\     5   \end{array} $ $ \begin{array}{c}     P \\     7 \\     5   \end{array} $ $ \begin{array}{c}     P \\     C = 13 \\     D = 13 \end{array} $
n (BUCI	(10) = n(B) + n(c) 6 = 13 + 13	+ $\eta(b) - \eta(BRC) - \eta(CRD) - \eta(BRB) + \eta(BRCRD)$ + 13 - $(2+x) - (4+x) - (3+x) + \chi$
2	8 = 39 - 2 - 7 - 4	4-x-3-x+x2=-2x
2	4 = 30 - 24	
0		1-2
<li>b) How many</li>	children have only one pet?	
-	7 + 6 + 5 = 18	

Г





HW: 3.4 p. 191-194 # 2, 4, 6, 7, 9, 11, 12 & 13

		Name	
		Date	
Goal: Un	derstand and interpret condit	tional statements.	
<ol> <li>conditional s school day."</li> </ol>	atement: An "if-then" stater	ment; for example, "If it is Monday, then it is a	
<ol> <li>hypothesis: school day," t</li> </ol>	An assumption; for example, i ne hypothesis is "It is Monday	in the statement "If it is Monday, then it is a y."	
3. conclusion: it is a school of	he result of a hypothesis; for ay," the conclusion is "it is a	example, in the statement "If it is Monday, then school day."	
<ol> <li>counterexam then it is a sch Thanksgiving</li> </ol>	ple: An example that disprov ool day" is disproved by the Monday. Only one counterext	ves a statement; for example, "If it is Monday, counterexample that there is no school on ample is needed to disprove a statement.	
5. <b>converse</b> : A switched; for school day, th	conditional statement in whic example, the converse of "If it en it is Monday."	h the hypothesis and the conclusion are t is Monday, then it is a school day" is "If it is a	
biconditional s number is even then it is even is divisible by	tatement is written as "p if ar n, then it is divisible by 2" is t " is also true. The biconditior 2."	nd only if q." For example, the statement "If a true. The converse, "If a number is divisible by 2, nal statement is "A number is even if and only if it	
$\begin{array}{c} \textbf{Commun}\\ p \Rightarrow q \text{ is no}\\ p \Rightarrow q \text{ is real} \end{array}$	cation Notation ation for "If p, then q." d as "p implies q."	CommunicationNotation $p \leftrightarrow q$ is notation for "p if and only if q."This means that both the conditional statementand its converse are true statements.	

LEARN ABOUT the Math James and Gregory like to play soccer, regardless of the weather. Their coach made this conditional statement about today's practice: "If it is raining outside, then we practise indoors.' When will the coach's conditional statement be true, and when will it be false? Example 1: Verifying a conditional statement (p.195) Verify when the coach's conditional statement is true or false. It is raining outside Hypothesis: \_ we practise indoors Conclusion: Each of these statements is either true or false, so to verify this conditional statement, consider four cases. Case 1: The hypothesis is true and the conclusion is true. It rains ostile and we practice indoors. When the hypothesis and conclusion are both true, a conditional statement is  $\pm$ rue Case 2: The hypothesis is false, and the conclusion is false. It does not rain outside and Le pratise outdoors When the hypothesis and conclusion are both false, a conditional statement is  $\pm r \mu e$ Case 3: The hypothesis is false, and the conclusion is true. It does not rown outside and we practice indoors When the hypothesis is false and conclusion is true, a conditional statement is  $\pm rue$ Case 4: The hypothesis is true, and the conclusion is false. - It rains outside and we practice outdoors When the hypothesis is true and conclusion is false, a conditional statement is <u>false</u> This Countrexample shows that the conditional statement is false

	Let q represent the conclusion: We practise indoors.
[	$p \qquad q \qquad p \Rightarrow q$
	TTT
د }	FFT
l	FTT
	TFF
7	When the hypothesis is false, regardless of whether the conclusion is true or false, the conditional statement is <b>true</b> From the truth table, I can see that the <b>only</b> time a <b>conditional statement</b> will be <b>false</b> is when the <b>hypothesis</b> is <b></b> and the <b>conclusion</b> is <b></b> .
Exam	ple 2: Writing conditional statements (p. 200)
"A per	son who cannot distinguish between certain colours is colour blind."
a)	White this contance as a conditional statement in Bif n, then all forms
а,	write this sentence as a conditional statement in "if $p$ , then $q$ " form.
а)	If a person cannot distinguish between certain colours
a)	If a person cannot distinguish between certain colours then that person is colour blind.
b)	If a person cannot distinguish between certain colours then that person is colour blind. Write the converse of your statement.
b)	If a person cannot distinguish between certain colours then that person is colour blind. Write the converse of your statement. If a person is colour blind then that person cannot distinguish half an parton colours.
b)	Af a person cannot distinguish between certain colours then that person is colour blind. Write the converse of your statement. If a person is colour blind then that person cannot distinguish between certain colours.
b) c)	Af a person cannot distinguish between certain colours then that person is colour blind. Write the converse of your statement. If a person is colour blind then that person cannot distinguish between certain colours. Is your statement biconditional? Explain.
b) c)	If a person cannot distinguish between certain colours then that person is colour blind. Write the converse of your statement. If a person is colour blind then that person cannot distinguish between certain colours. Is your statement biconditional? Explain. The first statement is <u>true</u>
b) c)	Write this sentence as a conditional statement in "IP, then q" form. If a person cannot dishingvish between certain colours then that person is colour blind. Write the converse of your statement. If a person is colour blind then that person cannot distinguish between certain colours. Is your statement biconditional? Explain. The first statement is <u>true</u> The converse is <u>true</u>
c)	Write this sentence as a conditional statement in "IFP, then q" form. If a person cannot dishingvish between certain colours then that person is colour blind. Write the converse of your statement. If a person is colour blind then that person cannot distinguish between certain colours. Is your statement biconditional? Explain. The first statement is <u>true</u> The converse is <u>true</u> The statement can be written:
c)	Write this sentence as a conditional statement in "it p, then q" form. If a person cannot distinguish between certain colours then that person is colour blind. Write the converse of your statement. If a person is colour blind then that person cannot distinguish between certain colours. Is your statement bloonditional? Explain. The first statement is <u>true</u> The converse is <u>true</u> The statement can be written:
с)	Write this sentence as a conditional statement in "IP, then d" form. If a person cannot distinguish between certain colours then that person is colour blind. Write the converse of your statement. If a person is colour blind then that person cannot distinguish between certain colours. Is your statement biconditional? Explain. The first statement is <u>thue</u> The converse is <u>true</u> The statement can be written: "A person is colour blind <u>If and only</u> <u>If</u> that person cannot distinguish between certain colours."
c)	Write this sentence as a conditional statement in "IFP, then q" form. If a person cannot dishingvish between certain colours then that person is colour blind. Write the converse of your statement. If a person is colour blind then that person cannot distinguish between certain colours. Is your statement biconditional? Explain. The first statement is <u>true</u> The converse is <u>true</u> The statement can be written: "A person is colour blind <u>If and only</u> <u>if</u> that person cannot distinguish between certain colours."

Example 5: Verifying a biconditional statement (p. 200)

Reid stated the following biconditional statement: "A quadrilateral is a square if and only if all of its sides are equal." Is Reid's biconditional statement true? Explain.

If a quadrilateral is a square then all of its sides are equal -> true Conditional Statement: If all the sides of a guadrilateral are equal Converse: then it is a square -> False counterexample: A rhombos hue 4 equal sides ... converse is fake Since the converse is false the biconditional statement is false.



F Math	12	3.6 The Inverse ar	nd the Contrapositive
		of Conditional St	atements_p. 208
			Name
			Date
	Goal: Un sta	derstand and interpret th tement.	ne contrapositive and inverse of a conditional
1. inv a c div	erse: A sta conditional s isible by 2,	atement that is formed by statement; for example, f ' the inverse is "If a numb	y negating both the hypothesis and the conclusion of or the statement "If a number is even, then it is ber is <b>not</b> even, then it is <b>not</b> divisible by 2."
2. co co a r by	ntrapositiv nclusion of iumber is ev 2, then it is	e: A statement that is fo the <b>converse</b> of a condit ven, then it is divisible by <b>not</b> even."	rmed by negating both the hypothesis and the tional statement; for example, for the statement "If 2," the contrapositive is "If a number is <b>not</b> divisible
p	q	$p \Rightarrow q$	Communication Notation
Т	Т	T	In logic notation, the inverse of "if p,
F	F	Т	then $q^{"}$ is written as "If $\neg p$ , then $\neg q$ ."
F	Т	Т	
Т	F	F	
		Communication In logic notation, t q" is written as "If	the contrapositive of "if $p$ , then f $\neg q$ , then $\neg p$ ."

a)	Verify the statement, or disprove it with a counterexample.			
	Hypothesis (p): Today is term. 29 Conditional statement: if p, then q.			
	Conclusion (q): This year is a leap year			
b)	Verify the converse, or disprove it with a counterexample.			
	converse: If this year is a leap year, then today is teb 29th			
	Hypothesis (1) g This year is a pap year Converse: if q, then p.			
	Conclusion (a): P Today 15 Feb 29th 8 P			
	$q \qquad p \qquad q \qquad q$			
	Cosmerexample. Toron 12 12015 7 F F			
C)	Verify the inverse, or disprove it with a counterexample.			
	Inverse: If today is not feb. 29th Then this is not a leap year			
	Hypothesis (¬p): Today is not Jeb. 27 Inverse: if ¬p, then ¬?			
	Conclusion (-q): This year is not a leap			
	$\gamma \partial \partial q$ $\neg p$ $\neg q$ pressure $\neg p$ $\neg q$			
	counter example: March 12th, 2013			
d)	Verify the contrapositive, or disprove it with a counterexample.			
	Contrapositive: IF This year is not a leap year, then beday is not less an			
	Hypothesis (¬q): This year is not a leap year Contrapositive: it g then ¬p.			
	Conclusion (-p): To day is not teb. 29th			
	TTT			



