

Name: \_\_\_\_\_

Date: \_\_\_\_\_

Block: \_\_\_\_\_

**Uncertainty**

(Giancoli 1.4)

**Uncertainty:** 8.8 cm has an estimated uncertainty of 0.1 cm in the measurement (one of the smallest fraction of the unit.)

$$\mathbf{8.8 \pm 0.1 \text{ cm}}$$

**Percent Uncertainty:** The ratio of the uncertainty to the measured value.

$$\frac{0.1}{8.8} \times 100\% \approx \mathbf{1\%}$$

$$\mathbf{8.8 \text{ cm} \pm 1\%}$$

**Calculations with Percent Uncertainty:**

To make calculations with uncertainty, you calculate first using the specified value, and second with the extreme value.

Ex: What is the area  $A$  of a circle of radius 12 m? What is the approximate uncertainty on the calculated area?

1. **Area (Specified):**  $A_{\text{Specified}} = \pi r^2 = \pi(12 \text{ m})^2 = 452 \text{ m}^2$

2. **Uncertainty:**  $12 \pm 1 \text{ m}$  (can be as low as 11 m or as high as 13 m)

3. **Area (Max):**  $A_{\text{max}} = \pi r^2 = \pi(13 \text{ m})^2 = 531 \text{ m}^2$

4. **Uncertainty on area:**  $\Delta A = A_{\text{max}} - A_{\text{Specified}}$   
 $= 531 \text{ m}^2 - 452 \text{ m}^2 = \mathbf{79 \text{ m}^2}$

5. **Percent Uncertainty:**  $\frac{\Delta A}{A_{\text{Specified}}} \times 100\% = \frac{79 \text{ m}^2}{452 \text{ m}^2} \times 100\% = \mathbf{17\%}$

Your answer (area of the circle):

$$\mathbf{452 \text{ m}^2 \pm 17\%}$$

- Write the following measurements with their uncertainty (Ex:  $6.4 \pm 0.1$  cm).
  - 1.67 m \_\_\_\_\_
  - 145 g \_\_\_\_\_
  - 12.004 kg \_\_\_\_\_
  - 1030 km \_\_\_\_\_
- Write the following measurements with their percent uncertainty. Round the percentage to a whole number. (Ex:  $4.32$  m  $\pm$  2% )
  - 1.67 m \_\_\_\_\_
  - $155 \pm 5$  g \_\_\_\_\_
  - $2000 \pm 100$  km \_\_\_\_\_
  - $100.0$  kg  $\pm$  0.1 kg \_\_\_\_\_
- Calculate the area, and the percent uncertainty, of a circle of radius  $1.3 \times 10^2$  cm?

\_\_\_\_\_ ( $53092$  cm<sup>2</sup>  $\pm$  16%)

- Calculate the volume, and the percent uncertainty, of a spherical beach ball whose radius is  $r = 3.86 \pm 0.08$  m?

\_\_\_\_\_ ( $241$  m<sup>3</sup>  $\pm$  6%)